

Name _____

4.2-4.3 Review

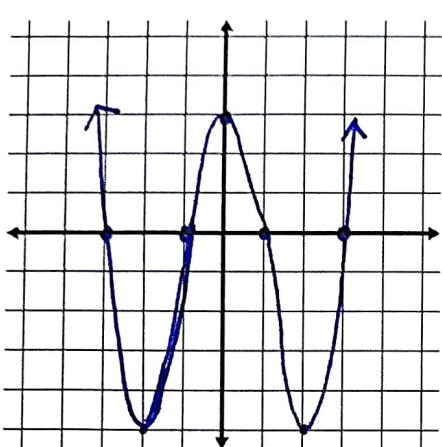
Date _____

Advanced Algebra

GRAPH EACH POLYNOMIAL FUNCTION. List the local max, local min, y-intercept, and end behavior of each.

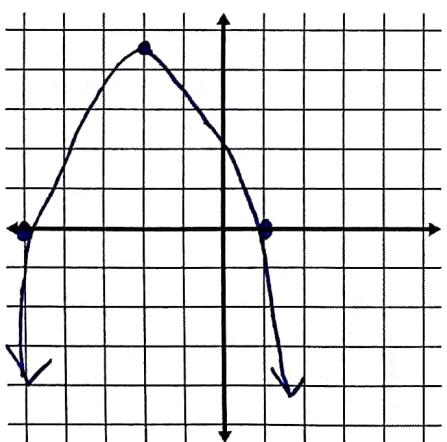
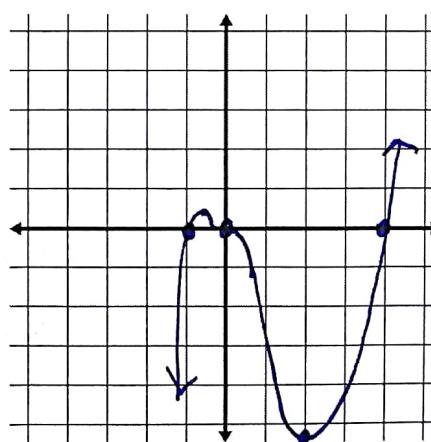
1) $f(x) = x^4 - 10x^2 + 9$; Roots = $\pm 3, \pm 1$

2) $f(x) = -x^3 + 13x + 12$; Roots = $-1, 4, -3$

Local max: (0, 9)Local Min: (-2, -15)y-intercept: (0, 9)EB: AS $x \rightarrow -\infty, f(x) \rightarrow \infty$.
AS $x \rightarrow \infty, f(x) \rightarrow \infty$ Local Max: (1.5, 28.1)Local Min: (-2, -6)EB: AS $x \rightarrow -\infty, f(x) \rightarrow \infty$.
AS $x \rightarrow \infty, f(x) \rightarrow -\infty$

3) $f(x) = -x^2 - 4x + 5$; Roots = $-5, 1$

4) $f(x) = x^5 - 3x^4 - 4x^3$; Roots = 0 mult. of 3, -1, 4

Local max: (-2, 9)Local Min: NONEy-intercept: (0, 5)EB: AS $x \rightarrow -\infty, f(x) \rightarrow -\infty$
AS $x \rightarrow \infty, f(x) \rightarrow -\infty$ (-2, 9)Local Max: (-0.5, 0.28)Local Min: (2, -48)y-intercept: (0, 0)EB: AS $x \rightarrow -\infty, f(x) \rightarrow -\infty$.
AS $x \rightarrow \infty, f(x) \rightarrow \infty$ (-0.5, 0.28)(2, -48)

Write a polynomial function that has the given zeros.

5) $\frac{3}{2}, -5 + 4i$

$$(2x-3)(x+5)$$

$$2x^2 + \cancel{10x} - 10x - 3x - 15$$

$$2x^2 + 7x - 15 = 0$$

6) $-1, 3 + \sqrt{5}i$
 $(x+1)(x-3)(x-5)$
 $x^2 - 3x + 1x - 3$

$$\begin{array}{c} x^2 - 2x - 3 \\ \hline x & | x^3 & -2x^2 & -3x \\ -5 & | -5x^2 & 10x & 15 \end{array}$$

$$x^3 - 7x^2 + 7x + 15 = 0$$

7) 0 mult. of 3, -3 mult. of 2, 5

$$x^3(x+3)(x+3)(x-5)$$

$$x^3(x^2 + 6x + 9)$$

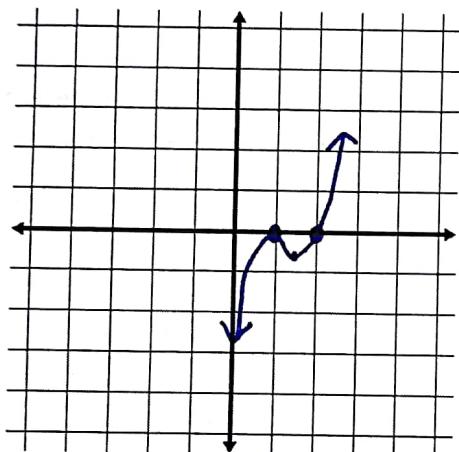
$$\begin{array}{c} x^5 + 6x^4 + 9x^3 \\ \hline x & | x^6 & 6x^5 & 9x^4 \\ -5 & | -5x^5 & -30x^4 & -45x^3 \end{array}$$

$$x^6 + x^5 - 21x^4 - 45x^3 = 0$$

Find all zeros of the following polynomial functions and graph. List the local max, local min, y-intercept, and end behavior of each.

8) $f(x) = x^3 - 4x^2 + 5x - 2$

given that 1 (mult. of 2), and 2 are roots



Roots: _____

Local Max: (1, 0)

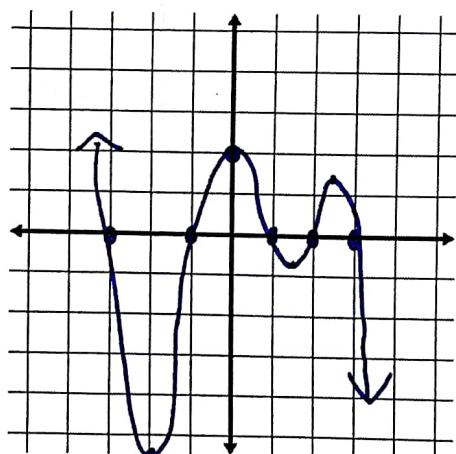
Local Min: (1.5, -0.125)

Y-int: (0, -2)

EB: AS $x \rightarrow -\infty, f(x) \rightarrow -\infty$
AS $x \rightarrow \infty, f(x) \rightarrow \infty$

(1.5, -0.125)

9) $f(x) = -x^5 + 2x^4 + 10x^3 - 20x^2 - 9x + 18$ given that 2, $\pm 3, \pm 1$ are roots



Roots: _____

Local Max: (0, 18) (2.5, 7.2) Local Min: (-2, -60) (1.5, -4.2)

Y-int: (0, 18)

EB: AS $x \rightarrow -\infty, f(x) \rightarrow \infty$.
AS $x \rightarrow \infty, f(x) \rightarrow -\infty$.

(-2, -60)

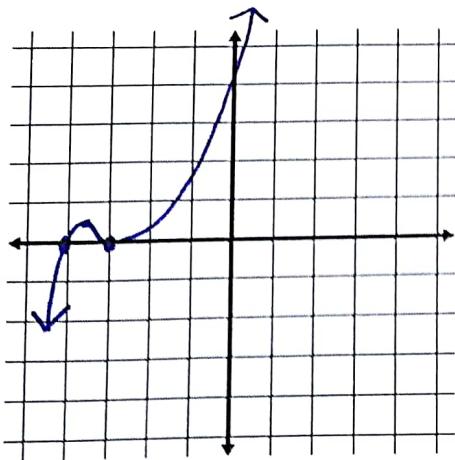
(0, 18)

(1.5, -4.2)

(2.5, 7.2)

11) $f(x) = x^3 + 10x^2 + 33x + 36$

given that -4 & -3 (mult. of 2) are roots



Roots: _____

Local Max: (-3.5, .125) Local Min: (-3, 0)

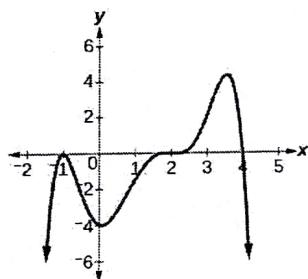
Y-int: (0, 36)

EB: As $x \rightarrow -\infty, f(x) \rightarrow -\infty$.
As $x \rightarrow \infty, f(x) \rightarrow \infty$.

(-3.5, .125)

Given the following graphs, determine whether the leading coefficient is positive or negative, and whether the degree is odd or even.

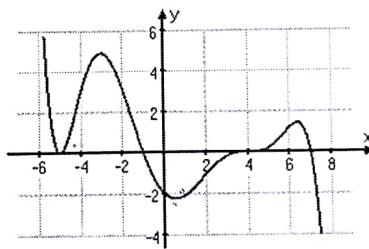
12)



LC: Neg

Deg: Even

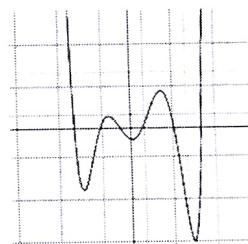
13)



LC: Neg.

Deg: Odd

14)



LC: Positive

Deg: Even