

Analytic Geometry
FBM #2 Study Guide
Chapters 1-9

Geometry FBM#2 – # of questions by topic

1. Properties → 1
2. Parallel lines (chapter 3) → 1
3. Congruent Triangles(chapters 4-5) → 3
4. Angles in a triangle → 3
5. Perpendicular/Angle Bisectors → 1
6. Parallelograms (chapter 7) → 6
7. Midsegment of a triangle → 1
8. Transformations → 1
9. Similar Triangles and proportional parts (chapter 8) → 4
10. Right Triangle trig (chapters 9-10) → 4

1. $TP = TP$ Reflexive
2. If $m < A = m < B$ and $m < B = m < C$, then $m < A = m < C$. Transitive
3. $2(x - 3) = 2x - 6$ Distributive
4. If $x = 8$, then $8 = x$. Symmetric
5. If $3x = 90$, then $x = 30$. Division
6. If $x = y$, then $x - 2 = y - 2$. Subtraction

7. The measures of the angles of a triangle are $m\angle A = 3x + 4$, $m\angle B = 2x$ and $m\angle C = 5x - 24$. Solve for x and $m\angle C$

$$3x + 4 + 2x + 5x - 24 = 180$$

$$10x - 20 = 180$$

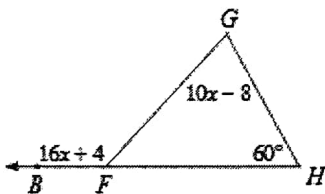
$$10x = 200$$

$$x = 20$$

$$m\angle C = 5(20) - 24$$

$$= 76^\circ$$

8. Find $m\angle G$



$$10x - 8 + 60 = 16x + 4$$

$$10x + 52 = 16x + 4$$

$$48 = 6x$$

$$x = 8$$

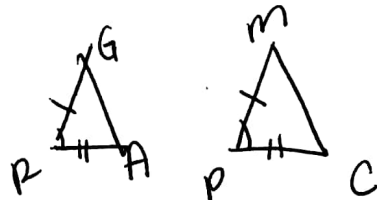
$$m\angle G = 10(8) - 8$$

$$= 80 - 8$$

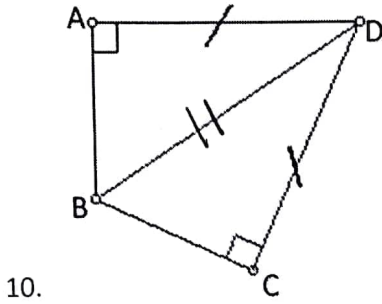
$$= 72^\circ$$

9. Given: $\triangle RGA$ and $\triangle PMC$ with $\overline{RG} \cong \overline{PM}$, $\overline{RA} \cong \overline{PC}$, and $\angle R \cong \angle P$. Which method could be used to prove that $\triangle RGA \cong \triangle PMC$? (Hint: Draw a picture)

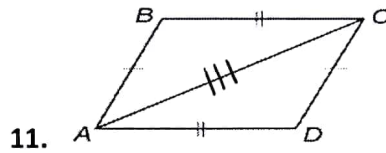
- a. SSS **b. SAS** c. HL d. ASA e. Not enough info.



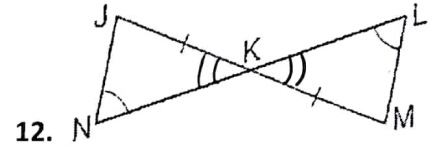
Determine if the triangles are congruent. MARK your diagrams! If so, write a congruency statement AND state the method of proving them congruent. If not, write "no congruence".



$\triangle ABD \cong \triangle CBD$
by HL



$\triangle ABC \cong \triangle CDA$
by SSS



$\triangle JNK \cong \triangle LMK$
by AAS

13.

$9x-1 + 10x+10 = 180$
 $19x+9 = 180$
 $19x = 171$
 $x = 9$

14.

$6x-10 = 50$
 $6x = 60$
 $x = 10$

15.

$17x+6 + 8x-1 = 180$
 $25x+5 = 180$
 $25x = 175$
 $x = 7$

16.

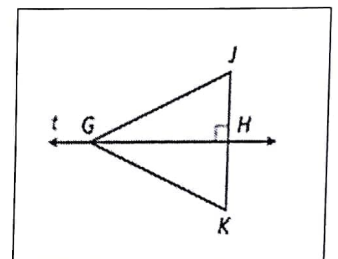
$4+18x = 17x+9$
 $x = 5$

17. Given that line t is the perpendicular bisector of \overline{JK} and $GK = 8.25$, find GJ 8.25

18. Given that line t is the perpendicular bisector of \overline{JK} , $JG = x + 12$ and $KG = 3x - 16$, and $JH = x - 7$, find KG and JH .

$x + 12 = 3x - 16$
 $28 = 2x$
 $x = 14$

$KG = 3(14) - 16 = 26$



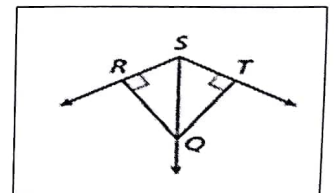
$JH = 14 - 7 = 7$

19. Given that $GJ = 70.2$, $JH = 26.5$, and $GK = 70.2$, find JK . 53

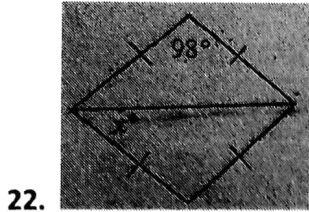
20. Given that $m\angle RSQ = m\angle TSQ$ and $TQ = 1.3$, find QR 1.3

21. Given that $m\angle RSQ = 58^\circ$, $RQ = 49$ and $TQ = 49$, find $m\angle RST$

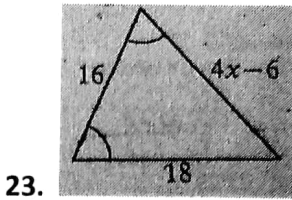
$58 \times 2 = 116^\circ$



For problems 22-23, find the value of x.



$$180 - 98 = \frac{82}{2} = \boxed{41^\circ}$$



$$4x - 6 = 18$$

$$4x = 24$$

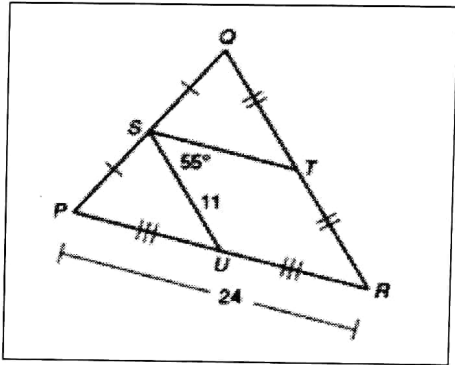
$$\boxed{x = 6}$$

Use the given diagram to answer questions 24 - 26.

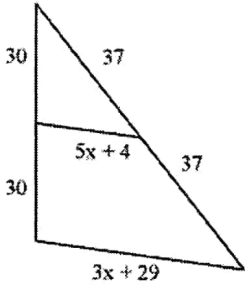
24. ST = $\boxed{12}$

25. PU = $\boxed{12}$

26. QR = $\boxed{22}$



27. Solve for x.



$$2(5x + 4) = 3x + 29$$

$$10x + 8 = 3x + 29$$

$$7x = 21$$

$$\boxed{x = 3}$$

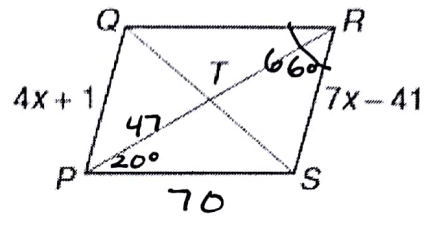
#'s 28-30 List the additional properties of the diagonals of the following parallelograms

28. Rectangle diagonals are \cong

29. Rhombus diagonals are \perp , diagonals bisect opp. \angle s

30. Square diagonals are \cong , diagonals are \perp , diagonals bisect opp. \angle s.

PQRS is a parallelogram. $PT = 47$, $PS = 70$, $m\angle SPT = 20^\circ$, and $m\angle QRS = 66^\circ$. Find each of the following measures.



31. RT 47

32. $180 - 66 = 114^\circ$
 $m\angle RSP$ 114°

33. QR 70

34. If $PT = 2x$ and $PR = 6x - 1$, find PT

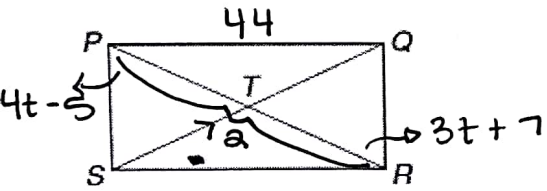
$2(2x) = 6x - 1$
 $4x = 6x - 1$
 $-2x = -1$
 $x = 1/2$
 $PT = 2(1/2) = 1$

35. $m\angle QPT$
 $66 - 20 = 46^\circ$

36. RS
 $4x + 1 = 7x - 41$
 $42 = 3x$
 $x = 14$

$RS = 7(14) - 41 = 57$

PQRS is a rectangle. $PQ = 44$, $PR = 72$, $m\angle SPT = (4t - 5)^\circ$, $m\angle QRT = (3t + 7)^\circ$. Find each of the following measures



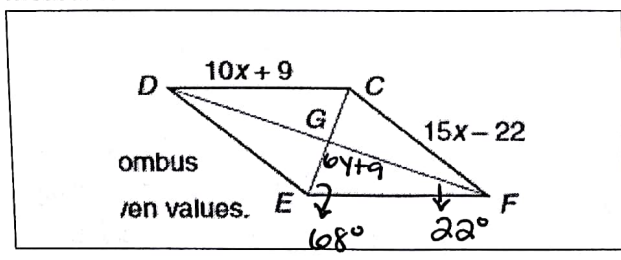
37. SR 44

38. $m\angle PSR$ 90°

39. TQ 36

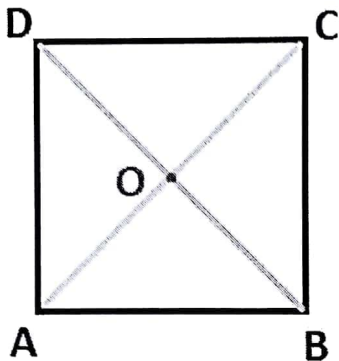
40. $m\angle QRP$
 $4t - 5 = 3t + 7$
 $t = 12$
 $3(12) + 7 = 43^\circ$

CDEF is a rhombus. The $m\angle EGF = (6y + 9)^\circ$, $m\angle GEF = 68^\circ$, and $m\angle GFE = 22^\circ$. Find each of the following measures.



41. x 6.2
 $10x + 9 = 15x - 22$
 $31 = 5x$
 $x = 6.2$
 42. EF 71
 $10(6.2) + 9 = 71$
 43. y 13.5
 $6y + 9 = 90$
 $6y = 81$
 $y = 13.5$
 44. $m\angle EFC$ 44°

Given square ABCD



45. If $m\angle ABC = 6x - 2$, solve for x

$$6x - 2 = 90$$

$$6x = 92$$

$$x = 46/3$$

46. If $m\angle ADO = 8x + 5$, solve for x

$$8x + 5 = 45$$

$$8x = 40$$

$$x = 5$$

47. If $AB = x + 5$ and $DC = 2x - 7$, Find BC

$$x + 5 = 2x - 7$$

$$12 = x$$

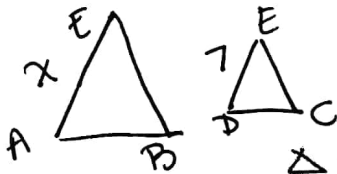
$$BC = 17$$

48. The scale factor ΔAEB to ΔDEC is 5:2. If $DE = 7$, then $AE = ?$

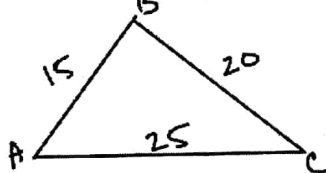
$$\frac{x}{7} = \frac{5}{2}$$

$$2x = 35$$

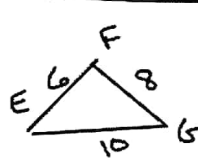
$$x = 17.5$$



$\Delta ABC \sim \Delta EFG$



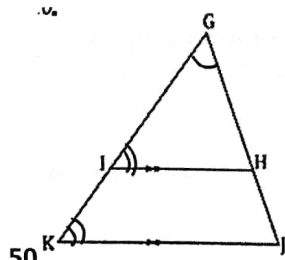
Scale Factor:



$$\frac{15}{6} = \frac{5}{2}$$

49. Find the scale factor:

Determine if the triangles are similar. List the parts, the postulate or theorem used, and if similar, write a similarity statement. If not similar, show enough work to prove why.



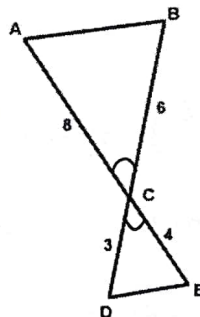
$$\angle G \cong \angle G$$

$$\angle GKH \cong \angle GHI$$

$$\Delta GKH \sim \Delta GHI$$

by AA

51.



$$\frac{AC}{EC} = \frac{8}{4} = 2$$

$$\frac{BC}{CD} = \frac{6}{3} = 2$$

$$\angle ACB \cong \angle ECD$$

$$\Delta ACB \sim \Delta ECD$$

by SAS

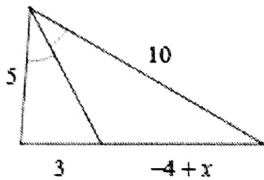
52. Find the value of x. $\frac{3x+7}{4} = \frac{x+3}{2}$

$$6x + 14 = 4x + 12$$

$$2x = -2$$

$$\boxed{x = -1}$$

53. Find x



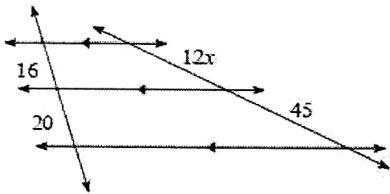
$$\frac{5}{10} = \frac{3}{-4+x}$$

$$30 = -20 + 5x$$

$$50 = 5x$$

$$\boxed{x = 10}$$

54. Solve for x.

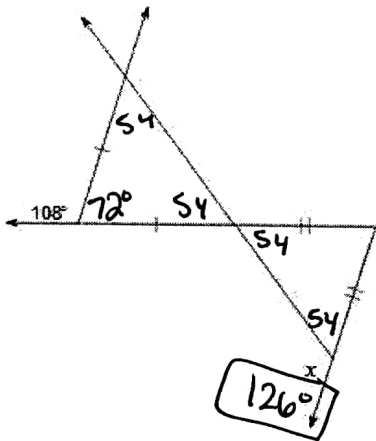


$$\frac{16}{20} = \frac{12x}{45}$$

$$240x = 720$$

$$\boxed{x = 3}$$

55. Solve for x.



56. Write the following formulas

a. Pythagorean Theorem (Right Triangle)

$$a^2 + b^2 = c^2$$

b. 45-45-90 L → H multiply by $\sqrt{2}$ H → L divide by $\sqrt{2}$

c. 30-60-90 SL → LL mult. by $\sqrt{3}$ LL → SL divide by $\sqrt{3}$
 SL → H mult. by 2 H → SL divide by 2

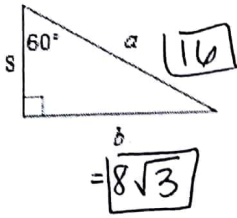
d. Trig Ratios

$$\sin \theta = \frac{\text{opp}}{\text{hyp}}$$

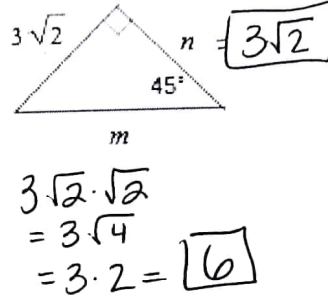
$$\cos \theta = \frac{\text{adj}}{\text{hyp}}$$

$$\tan \theta = \frac{\text{opp}}{\text{adj}}$$

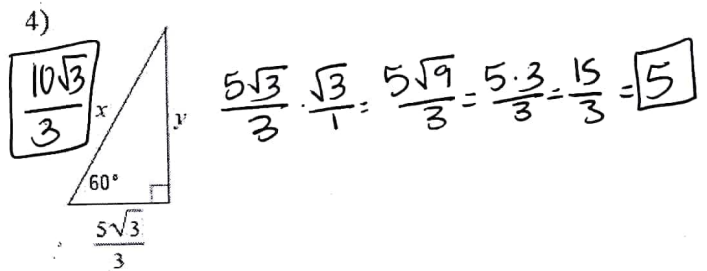
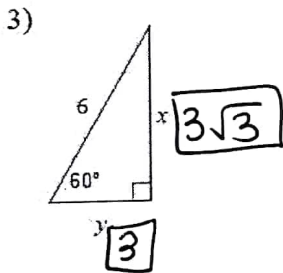
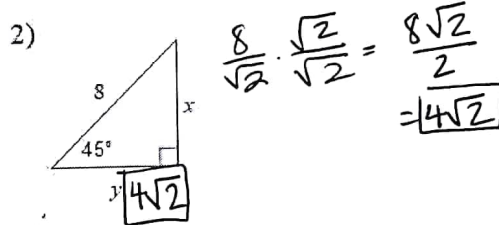
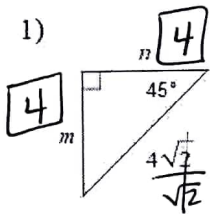
57. Find the missing sides.



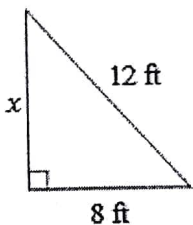
58. Find the missing sides.



Find the missing side lengths. Leave your answers as radicals in simplest form.



63. Find the missing side in simplified radical form

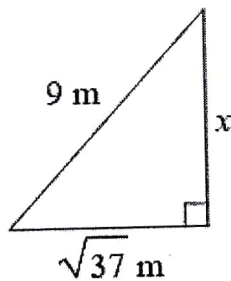


$$x^2 + 8^2 = 12^2$$

$$x^2 + 64 = 144$$

$$\sqrt{x^2} = \sqrt{80}$$

$$x = 4\sqrt{5} \text{ ft}$$

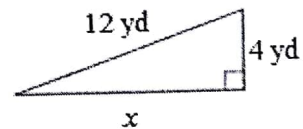


$$\sqrt{37}^2 + x^2 = 9^2$$

$$37 + x^2 = 81$$

$$\sqrt{x^2} = \sqrt{44}$$

$$x = 2\sqrt{11} \text{ m}$$



$$x^2 + 4^2 = 12^2$$

$$x^2 + 16 = 144$$

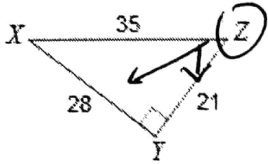
$$\sqrt{x^2} = \sqrt{128}$$

$$x = 8\sqrt{2} \text{ yd}$$

Express answers as a ratio and a decimal.

64.

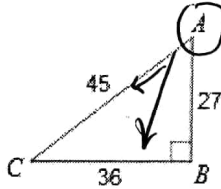
$\tan Z$



$$\tan Z = \frac{28}{21} = \boxed{\frac{4}{3}}$$

65.

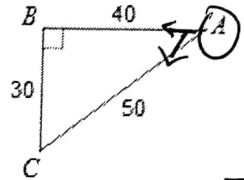
$\sin A$



$$\sin A = \frac{27}{45} = \boxed{\frac{3}{5}}$$

66.

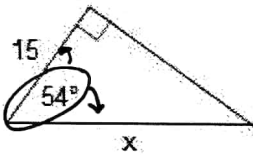
$\cos A$



$$\cos A = \frac{40}{50} = \boxed{\frac{4}{5}}$$

Find the missing side. Round to the nearest tenth.

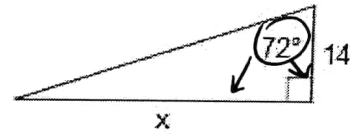
1)



$$\cos 54 = \frac{15}{x}$$

$$x = \frac{15}{\cos 54} = \boxed{25.5}$$

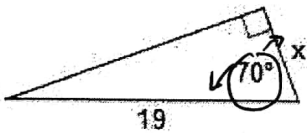
2)



$$\tan 72 = \frac{14}{x}$$

$$x = \boxed{43.1}$$

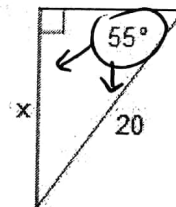
3)



$$\cos 70 = \frac{x}{19}$$

$$x = \boxed{6.5}$$

4)



$$\sin 55 = \frac{x}{20}$$

$$x = \boxed{16.4}$$