

Extending Number System Test REVIEW

Simplify.

1) $\sqrt{24} < \frac{4}{4} \left(\frac{2}{2}\right)$

$2\sqrt{6}$

2) $-8\sqrt{18} < \frac{9}{2} \left(\frac{3}{3}\right)$

$-24\sqrt{2}$

3) $7\sqrt{20} < \frac{4}{5} \left(\frac{2}{2}\right)$

$14\sqrt{5}$

4) $7\sqrt{448} < \frac{4}{112} \left(\frac{4}{4}\right) < \frac{4}{28} < \frac{4}{7} \left(\frac{2}{2}\right)$

$56\sqrt{7}$

5) $2\sqrt{2} - \sqrt{2} = 2\sqrt{2} - \sqrt{3}$

$-\sqrt{2} - \sqrt{3}$

6) $\sqrt{8} + \sqrt{2}$

$2\sqrt{2} + \sqrt{2} = 3\sqrt{2}$

7) $2\sqrt{18} + 3\sqrt{8}$

$6\sqrt{2} + 6\sqrt{2} = 12\sqrt{2}$

8) $-\sqrt{27} - \sqrt{45} - \sqrt{27}$

$-6\sqrt{3} - 3\sqrt{5}$

9) $-4\sqrt{20} \cdot \sqrt{5}$

$-4\sqrt{100}$

-40

10) $-5\sqrt{5} \cdot 2\sqrt{5}$

$-10\sqrt{25}$

-50

11) $\sqrt{6}(-3\sqrt{2} - 4\sqrt{6})$

$-3\sqrt{12} - 4\sqrt{36}$

$-6\sqrt{3} - 24$

12) $\sqrt{6}(\sqrt{3} + \sqrt{5})$

$\sqrt{18} + \sqrt{30}$

$3\sqrt{2} + \sqrt{30}$

$$13) (-5\sqrt{5}-1)(\sqrt{5}+5)$$

$$-5\sqrt{5}\sqrt{5} - 25\sqrt{5} - \sqrt{5} - 5$$

$$-25 - 26\sqrt{5} - 5$$

$$\boxed{-30 - 26\sqrt{5}}$$

$$14) (2\sqrt{3}+2)(\sqrt{3}-2)$$

$$2\sqrt{3}\sqrt{3} - 4\sqrt{3} + 2\sqrt{3} - 4$$

$$6 - 2\sqrt{3} - 4$$

$$\boxed{2 - 2\sqrt{3}}$$

$$15) (-4\sqrt{3}-2)(5\sqrt{3}-3)$$

$$-20\sqrt{3}\sqrt{3} + 12\sqrt{3} - 10\sqrt{3} + 6$$

$$-60 + 2\sqrt{3} + 6$$

$$\boxed{-54 + 2\sqrt{3}}$$

$$16) (-1+\sqrt{3})(-5+\sqrt{3})$$

Determine if the result is a rational or irrational number and explain why.

$$17) -2\sqrt{45} + 3\sqrt{20}$$

$$\begin{matrix} \hat{9} & \hat{4} \\ \downarrow & \downarrow \\ 3\sqrt{5} & 2\sqrt{5} \end{matrix}$$

$$-6\sqrt{5} + 6\sqrt{5}$$

$$0 \quad \boxed{\text{Rational}}$$

$$18) \sqrt{6}(\sqrt{6}+3)$$

$$\sqrt{36} + 3\sqrt{6}$$

$$6 + 3\sqrt{6} \leftarrow \text{non perfect square}$$

$$\boxed{\text{Irrational}}$$

Simplify each expression.

$$19) (4 - 2n^4 + 8n) + (8n^5 - 2n^3 + 3 + 4n^2) + (3n^3 - 6n^2)$$

$$2n^5 - 2n^4 + n^3 + 4n^2 + 8n + 7$$

$$20) (5x^5 + 5x^4) - (-6x^4 + 3x^5)$$

$$2x^5 + 11x^4$$

$$21) (2 - 7m^2 - 7m^4 - 7m) + (-7m^2 - 5 + 4m - 5m^4) - (4m + 7m^2 - 1 + 3m^4)$$

$$-15m^4 - 21m^2 - 7m - 2$$

Find each product.

22) $5(4n - 1)$

$20n - 5$

23) $(6n + 8)(3n + 2)$

$18n^2 + 12n + 24n + 16$

$18n^2 + 36n + 16$

24) $(6a - 2)(5a - 4)$

$30a^2 - 24a - 10a + 8$

$30a^2 - 34a + 8$

25) $(7p + 7)(6p + 5)$

$42p^2 + 35p + 42p + 35$

$42p^2 + 77p + 35$

26) $(4n + 7)(8n^2 + 4n - 1)$

4n	$32n^3$	$16n^2$	$-4n$
7	$28n^2$	$28n$	-7

$32n^3 + 72n^2 + 24n - 7$

27) $(8v - 2)(7v^2 + 6v + 2)$

	$7v^2$	$+ 6v$	$+ 2$
8v	$56v^3$	$48v^2$	$16v$
-2	$-14v^2$	$-12v$	-4

$56v^3 + 34v^2 + 4v - 4$

28) $(8x - 1)(6x^2 - 3x + 6)$

	$6x^2$	$-3x$	$+ 6$
8x	$48x^3$	$-24x^2$	$48x$
-1	$-6x^2$	$3x$	-6

$48x^3 - 30x^2 + 51x - 6$

29) $(3x + 3)(7x^2 + 4x + 2)$

	$7x^2$	$+ 4x$	$+ 2$
3x	$21x^3$	$12x^2$	$6x$
3	$21x^2$	$12x$	6

$21x^3 + 33x^2 + 18x + 6$

30) $(-3v^2 + 8v - 6)(-7v^2 - 4v - 4)$

	$-7v^2$	$-4v$	-4
$-3v^2$	$21v^4$	$12v^3$	$12v^2$
8v	$-56v^3$	$-32v^2$	$-32v$
-6	$42v^2$	$24v$	24

$21v^4 - 44v^3 + 22v^2 - 8v + 24$

31) $(-5r^2 - r + 7)(8r^2 - 2r + 4)$

	$8r^2$	$- 2r$	$+ 4$
$-5r^2$	$-40r^4$	$10r^3$	$-20r^2$
$-r$	$-8r^3$	$2r^2$	$-4r$
7	$56r^2$	$-14r$	28

$-40r^4 + 2r^3 + 38r^2 - 18r + 28$

32) $(-6v^2 + v - 6)(-4v^2 - 8v - 3)$

	$-4v^2$	$-8v$	-3
$-6v^2$	$24v^4$	$48v^3$	$18v^2$
v	$-4v^3$	$-8v^2$	$-3v$
-6	$24v^2$	$48v$	18

$24v^4 + 44v^3 + 34v^2 + 45v + 18$